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Sideways crab-walking is faster and more efficient than forward walking for a hexapod robot

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Abstract

PAPER

Articulated legs enable the selection of robot gaits, including walking in different directions such as forward or sideways. For longer distances, the best gaits might maximize velocity or minimize the cost of transport (COT). While animals often have morphology suited to walking either forward (like insects) or sideways (like crabs), hexapod robots often default to forward walking. In this paper, we compare forward walking with crab-like sideways walking. To do this, a simple gait design method is introduced for determining forward and sideways gaits with equivalent body heights and step heights. Specifically, the frequency and stride lengths are tuned within reasonable constraints to find gaits that represent a robot's performance potential in terms of speed and energy cost. Experiments are performed in both dynamic simulation in Webots and a laboratory environment with our 18 degree-of-freedom hexapod robot, Sebastian. With the common three joint leg design, the results show that sideways walking is overall better (75% greater walking speed and 40% lower COT). The performance of sideways walking was better on both hard floors and granular media (dry play sand). This supports development of future crab-like walking robots for future applications. In future work, this approach may be used to develop nominal gaits without extensive optimization, and to explore whether the advantages of sideways walking persist for other hexapod designs.

1. Introduction

Legs enable animals [1, 2] and robots [3–26], to navigate particularly challenging terrains. Bio-inspired multi-legged robots [27–29], have shown how using many legs together in a coordinated gait results in fast and stable locomotion. In particular, our group is inspired by crabs which can cross a spectrum of wet to dry sandy terrains and small to large rocks [30, 31].

Many legged robots, inspired by insects, are hexapods that walk forward. Statically stable gaits can be generated with inverse kinematics [32]. Stability margins can be quantified based on center of mass (COM) location relative to the support polygon [33–36].

Contact forces can be used to generate adaptive gaits [37–39]. Dynamic control can achieve desired task accelerations [40]. Bioinspired controllers have demonstrated stable walking through the translation of biological concepts such as central pattern generators [41], genetic algorithms [42], artificial

neural networks [43], and spiking neural networks [44, 45]. Forward walking has been demonstrated to be predictable enough for planning [46], simultaneous localization and mapping [47], and walking in confined spaces [48].

Sideways walking has been studied in a relatively smaller number of robots. One important exception in bipeds [49] shows that rotating the hips and knees to operate in the sagittal plane with a nonanthropomorphic gait is akin to walking sideways and reduces roll oscillations [50]. In this design, adding rotation at the hip is best for steering, resulting in a biped leg design that is similar to a crab leg [51]. A robot with four legs that operates this way can switch between quadruped gaits and biped stances [52]. A second important exception is in omni-directional legged gaits [53-55], where robots might use sideways walking to side-step an obstacle or stabilize a lateral perturbation. Others have characterized the stability of sideways walking with dynamic gait stability margins [56] and minimization of foot forces and torques [57].

Robots inspired by crustaceans are especially promising in traversing amphibious terrain. While lobster-like robots with eight legs walk forward in water [26], the crab-like hexapod Ariel walks sideways on land or underwater with invertible legs [3]. Forward bounding gaits have been demonstrated with a swimming quadruped crab-like robot [58]. Sideways walking can be accomplished with compliant reduced-actuated legs in flat and sloped terrain [25]. More recently, Crabster and little Crabster robots have been designed to traverse deep and shallow water, respectively [19, 20, 59, 60]. As amphibious legged robots become more advanced, sideways walking may become more important.

While most engineered robots default to a forward walking gait [17, 18, 30–40, 42–48, 61, 62], most biological crabs default to sideways walking [63, 64]. Furthermore, crab species that develop sideways walking (carcinization) [65] are thought to do so to increase speed [66]. Should crab-like robots walk sideways as well? Or are the mechanics of robots sufficiently different that forward walking is always better? For future robots to traverse the types of terrains that biological crabs excel in, which is better? To our knowledge, direct comparisons between forward and sideways hexapod walking have not been done in robotics and are needed to answer the preceding questions.

In this paper, our goal is to compare forward and sideways walking for a robot that can do both. We propose a simple, direct method for finding a gait that represents the robot's performance potential for a particular walking direction. The robot's workspace first is computed and used to define end effector paths for each leg that utilize their longest feasible stride lengths (SLs) in a particular direction. Then, dynamic simulation is used to iteratively find the minimum leg cycle time for which the paths can be followed with a desired accuracy, resulting in a gait that is both efficient and accurate. This allows us to directly compare velocity and energy usage at different walking heights and SLs for forward and sideways walking, first in simulation, and then on a mobile robot. The simulation platform is Webots [67-69], a widely used and validated robot simulation software [70-76]. The hardware platform is our robot Sebastian [77], figure 1(a), walking on flat ground and in sand. Finally, practical trade-offs of sideways and forward walking are discussed. In future work, this method can be applied to other types of robots to determine appropriate nominal walking gaits and further understand crab-like gaits with robot models.

2. Relationship to other legged gait literature

Analytical research has shown how factors such as velocity, body height, SL, duty factor, joint torque, viscosity, and heat loss can be used to minimize energy cost [78, 79]. For example, smaller duty factors can improve energy cost when speed is increased [80, 81]. However, if the duty factor is too low (<0.5) the robot can become unstable if there are fewer than three legs on the ground at a given time. Thus, in this paper, we assume an alternating tripod gait, common to many other hexapod robots [76, 82–90], which can be generalized to other alternating stance gaits for four or more legs.

Other researchers show that uniformly distributing vertical ground reaction forces results in improved energy efficiency [91]. Even if the ground reaction forces cannot be used in the optimization, minimizing the sum of the squares of joint torques improves the distribution of foot forces and moments [92–95]. Thus, a torque distribution algorithm has been shown to decrease the proportion of heat loss and, as a result, decrease energy cost [96].

It is also possible to use numerical methods to improve gaits over time. For example, using a genetic algorithm [97] to optimize the controller with respect to energetic efficiency, travelled distance and stability of the robot locomotion [98]. More recent robots have shown promise in developing gaits with end-toend deep learning [44]. A full review can be found in [99]. However, these energy-based strategies can be time consuming, or have uncertainty about achieving a solution, or cannot easily and directly be applied to other articulated legged robots [99].

In the present work, our gait design method is based on the observation that longer SLs often help both speed and energy cost. Detailed animal simulations [80] suggest that to achieve high speed walking with maximum efficiency, longer SLs should be used. Human velocity measured on a treadmill shows that SL changes linearly with velocity outside the transition area [100]. While [80] also suggests there is an optimal stride and swing period for a given velocity, we allow these to vary in our method in order to follow the planned end effector trajectories with a desired accuracy. Thus, our gait design method differs from the existing literature in that while the resulting gaits are not optimized for speed or energy cost, they can be expected to be relatively fast and efficient while following their planned leg trajectories accurately. These modifications allow for their use to compare the robot's performance in different walking directions.

3. Hardware and simulation platforms

We validate our results on our crab-like robot Sebastian, figure 1(a), which has physical parameters listed in table 1. This robot's leg design is loosely inspired by the biological crab species *Pachygrapsus crassipes*, which is a small shore crab that typically walks sideways. Like crabs, the legs end in pointed dactyls [30, 31]. However, while shore crabs are often 5 cm long, our robot is scaled up to 33 cm long to accom-



modate standard SAVOX SV-1270TG motors. Also, the robot is a hexapod in order to have the minimum number of legs for an alternating tripod gait. Thus, there are 18 degree-of-freedom (DOF). All of the leg pieces are 3D printed (MarkerGear M2, PLA, 100% infill). The orange chassis contains batteries and electronics for control and data collection. The robot uses a Raspberry Pi 4B powered by a PiSugar2 Pro as its on-board CPU, which communicates with an 18-pin Pololu Maestro servo controller. A 7.4 V lithium polymer battery powers the motors, and an INA260 power sensor measures the power draw at 25 Hz. The sensor measurements are collected with an Arduino Nano and sent to the on-board CPU.

We use a simplified model in Webots simulation as shown in figure 1(b). Webots is a robotics platform that can model, program and simulate mobile robots with a large number of available sensors and actuators [67-69]. It is used widely in robotics simulation and has been validated in several relevant examples [70-76], with results which are relevant to our study.

Table 1.	Robot	dim	ensions.
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	Length (cm)	Weight (g)
Total robot	33 ^a	3650
Body	20 ^b	1800
$1 \cos(L_1)$	5.4	21.8
1 femur (L ₂ , 1 servo included)	9.0	95.0
1 tibia (L ₃ , 2 servos included)	7.5	176.9
1 dactyl (L ₄)	12.6	16.6

^aThe minimum length of Sebastian in *Y* direction (figure 1(a)), when the robot is standing.

^bThe length of Sebastian in X direction (figure 1(a)).

4. Gait design method

Here, the goal of our gait design method is to find fast, stable and low cost of transport (COT) gaits for robots that have articulated legs. Specifically, a common articulation design (e.g. [6-10, 18, 30, 31, 37]) is to have a 'hip' joint that rotates the leg about a vertical axis, followed by 'knee' and 'ankle' joints that have parallel and horizontal axes of rotation, figure 1(c). Note that human and animal 'hip' joints can rotate in multiple directions, but typical servomotors only rotate in one direction, so this nomenclature is a convenience for this paper. The critical design parameters are the length of the segments between these joints. With such a design a robot can walk at a range of body heights (in Z-direction, figures 1(a) and (b)) and at a range of different step sizes and step heights. A typical forward walk (in X-direction, figures 1(a) and (b)) will involve using broad motions of the hip to move forward and smaller adjustments of the knee and ankle to maintain a straight stride. A sideways walk (in Y direction, figures 1(a) and (b)) will involve greater motions at the knee and ankle to maintain constant height, with only small motions at the hip if steering is required.

To compare forward and sideways gaits, our method, shown in figure 2, maximizes SL and frequency (reciprocal of period (T)) sequentially at a desired height. Subject to our constraints, this should approximately maximize the velocity (v) based on equation (1)

$$v = 2 * \frac{\mathrm{SL}}{T}.$$
 (1)

*Specifically, when the root-mean-square error (RMSE) between measured and commanded trajectory is ≤ 1.2 cm, swing height error (e_{HS}) is $\leq 7\%$, and SL error (e_{SL}) is $\leq 9\%$, section 4.3.

Firstly, we calculate the workspace at the desired height and select the longest strides possible within the workspace (either in *X* direction for forward or in *Y* direction for sideways walking, figure 3(a)). This is expanded upon in section 4.1.

Secondly, we apply inverse kinematics to find the joint angles for a trajectory with stance that follows full SL and swing that follows a parabolic arc with set height (figures 3(b) and (c) and 4(a) and (b)) in section 4.2.

Thirdly, we simulate in Webots with the planned trajectory and the joint angles with position control in section 4.2, discussed in section 5.

Fourthly, we check if the measured simulated legs in Webots follow the commanded trajectory accurately by tuning the period. We increase the stepping period to decrease the velocity or increase the number of points k (section 4.2) until the robot follows the desired trajectory within a defined threshold of error. This is expanded upon in section 4.3.

Finally, we validate the key results on Sebastian. These results are shown in section 6.

4.1. Finding workspace and stride

Just like biological crabs, our robot's joints have rotational limits, which together with the leg lengths determine the reachable space (workspace) of the dactyl. Joint limits are partly due to interference between the proximal and distal segments if they rotate too far. In addition, servos themselves have rotation limits. Our robot's dactyls intentionally point inward [30, 31] and are therefore not reversible. As shown in figure 4(a), the rotational range for hip joints θ_1 is (-22.5°, 22.5°) and for knee joints θ_2 (-80°, 20°), and for ankle joints θ_3 (-130°, 0). The negative value for θ_1 is the clockwise direction, and the negative values for θ_2 and θ_3 are the downward direction. The 0° for hip joints is shown with bold dark lines in figure 3(b).

We also limit the workspace based on the angle between the ground and the dactyl (AGD) for stable walking, figure 4(a). We consider the AGD to be zero when the dactyl is normal to the ground (vertical). When the dactyl points inward toward the body, the AGD is negative. When the dactyl points outward away from the body, the AGD is positive. The workspace is thus constrained to AGD ranges $(-60^\circ, 60^\circ)$. Larger (positive) AGD results in an excessively sprawled posture and a tendency to slip on flat surfaces. At this AGD range, the robot can successfully extract dactyls at each swing.

In order to have room to walk forward, the middle legs are normal to the body and the front and rear legs are rotated 45° with respect to normal to the body, see figure 3(b). Sideways walking gait uses a configuration where the legs are parallel to each other, as shown in figure 3(c). The workspace in figure 3(a) is determined by forward kinematics with rotational angles' limitations and leg lengths shown in table 1. The height, *h*, is the distance between the knee rotational axis and the tip of the dactyl. The *XY* plane shows the workspace with a given height.

Except where indicated, we choose 17.5 cm as the desired height. This height is the minimum for our physical robot testing because of the sprawl limits, sinkage in sand, and the clearance between the body and the ground. With the given height, the workspace of the right front, middle and rear legs for forward walking is shown in figure 3(b) in gray. The left legs workspaces (not shown) are symmetrical with the right legs. Then, we find the full SL for the gait, the red lines in figure 3(b). Based on geometry, figure A1 in appendix A, the full SL for the right front, middle and rear legs are the same. Figure 3(c) is the workspace for sideways walking, as legs are parallel and the hip joints are not used. The full SL is 15 cm. The gray shape shows the available workspace. The blue (green) displays the full stride (half stride) for sideways walking. Note that the half stride experiments are performed with the distal part of the workspace, because it is more stable.

4.2. Trajectory inverse kinematics

In both forward walking and sideways walking, the stance phase trajectory is a straight line and the swing phase trajectory is a parabola with 6 cm swing height,



as in figure 4. We choose 6 cm as the swing height, because this is sufficient for extracting dactyls from the sand. A higher swing will be able to step over larger obstacles, but will cost more energy during the swing phase and may slow the required stepping frequency. A RMSE analysis of the simulated end effector trajectory, found that 66% of the trajectory error for forward walking occurs in the swing phase. Consequently, we expect an increase in the swing height to result in a decrease in speed. Similarly, about 55% of the trajectory error sideways walking is in the swing phase, so we expect increasing the swing height to decrease speed. Figure 4(a) is the trajectory for the right middle leg for forward walking and figure 4(b) is the trajectory for the right legs' sideways walking.

First, we use inverse kinematics to determine joint angles required for points along the path. Then, we use polynomial fitting to generate the trajectory for Webots simulation (with convergence criteria of $R^2 \ge 90\%$).

In stance, the trajectory, figure 4, is defined by endpoints A and B, which are determined by the full stride in figures 3(b) and (c). We divide the stride into k equal segments of equal time. At each of the resulting k + 1 points, we use inverse kinematics to find the joint angles, then use polynomial interpolation to determine the desired joint angles (θ_1 , θ_2 , and θ_3) as a function of time for position control. We start with k = 9, and increase it as described in section 4.3 and figure 2.

In forward walking swing phase, the hip angle (θ_1) increases at a constant rate and we use inverse kinematics to determine the knee and ankle angles $(\theta_2 \text{ and } \theta_3)$ that keep the end effector on the desired parabolic trajectory, figure 4. Thus the k + 1 points are determined by increments of $(\theta_{1B} - \theta_{1A})/k$, where θ_{1B} and θ_{1A} are the θ_1 for point B and A respectively, figure 4. In sideways walking swing phase, the *x* direction speed is held constant and thus the k + 1 points are determined by increments of $(x_B - x_A)/k$, where x_B and x_A are the *x* positions for points B and A respectively, figure 4.

4.3. Period tuning

After determining the trajectory with inverse kinematics, we determine the fastest possible frequency for an accurate step. In order to compare forward and sideways walking with equivalent metrics, we set a threshold for the end effector trajectory accuracy. Specifically, we chose 8% of the full SL, which is 6% of Sebastian's body length, and 4% of Sebastian's leg length. When the robot cannot keep up with the desired trajectory within the threshold, the speed is too fast. In addition, we choose the criteria for margin of error of swing height (Δ Hs \leq 7%) and SL (Δ SL \leq 9%). Except where indicated, the periods used for all the gaits in this paper are based on this method.

Periods are evaluated iteratively in Webots simulations. For each period, the x, y, and z coordinates of the end effector are measured and compared with the commanded trajectory, with 33.3 Hz as the sampling frequency. If the RMSE is less than 1.2 cm, the



Figure 3. The workspace of the dactyl tip (a) determines the available SL for walking (b) forward or (c) sideways. The black lines in (a) represent the height chosen to figure out the effect of height. Note that for comparison, we consider a half-stride sideways walk (green) in (c) that uses only the distal part of the workspace (gray) because that results in more stable walk.

speed is increased. If RMSE, e_{SL} and/or e_{HS} thresholds are exceeded, the period *T* or the number of points *k* is increased; if RMSE exceeds 1.2 cm, the period *T* is increased; and if e_{SL} and/or e_{HS} exceeds the defined thresholds, *k* is increased, according to figure 2. The resulting period is used for the simulation and validation gaits.

This process is demonstrated numerically in table 2. Here we show that for forward walking we can use a smaller period, decreasing until the normalized RMSE (the RMSE divided by the threshold) exceeds 100%. Thus, the period we selected was 1.44 seconds.

Similarly for sideways walking, the periods are longer (and the SLs are also longer).

Note that the period resolution (0.18 seconds in table 2) is sufficiently small since the maximum velocity error from the period resolution ($<0.03 \text{ m s}^{-1}$) is smaller than the difference between the maximum velocities (0.085 m s⁻¹) for sideways and forward walking. Furthermore, since we can analytically predict the velocity using equation (1), we can further show that the theoretical error would be less than the reported differences between maximum sideways and forward velocities.



Figure 4. In both forward (a) and sideways (b) walking, the stance trajectory is a straight line (green) and the swing trajectory is a parabola with height Hs = 6 cm.

 Table 2.
 RMSE between measured simulated trajectory and commanded trajectory and simulation velocity

 with different periods for full stride forward and sideways walking—the stride for forward walking is 14 cm

 and sideways walking 15 cm. *T* is the period. The bold data is the proper periods we choose.

Forward walking	Period T (s)	1.8	1.62	1.44	1.26	1.08
	Normalized RMSE	102%	96%	90%	105%	113%
	Velocity (m s ⁻¹)	0.109	0.105	0.116	0.134	0.153
Sideways walking	period T (s)	2.4	1.86	1.68	1.5	1.32
	Normalized RMSE	91%	94%	95%	88%	100%
	Velocity (m s ⁻¹)	0.132	0.166	0.186	0.200	0.227

5. Simulation preliminary results

The gaits used in both forward and sideways walking are tripod gaits. In Webots, the robot is walking on a linoleum floor where the friction coefficient is 0.5. The velocity is measured from total position, d, moved after ten full steps, and excludes the steps before the first 0.3 seconds, to eliminate acceleration transients. The position is obtained from the GPS node in Webots. Energy consumption, E, is measured by the battery node. COT is calculated based on equation (2)

$$COT = \frac{E}{mgd}$$
(2)

where *g* is the acceleration of gravity and *m* is the mass of the robot.

5.1. Effect of stride length

Our Webots simulation confirms that using the longest SL results in the fastest and the most efficient gaits, figure 5. At the chosen height of 17.5 cm, we compared behavior with shorter strides. In sideways walking, with a full SL of 15 cm, we consider the most

distal portions of the SL to take shorter strides. In forward walking, with a full SL of 14 cm, the middle leg strides are centered while the front and rear legs are spaced as far as possible from the middle leg (forward and rear parts of the full SL). Decreasing SL monotonically decreases velocity and increases COT until steps are smaller than the step height. At these small SLs, the robot is even slower and less efficient.

Furthermore, it is clear that sideways walking is almost twice as good, both in speed and efficiency for a given SL. Thus, a sideways walk with a half stride (7.5 cm) should be more efficient than a forward walk with a full 14 cm stride. This hypothesis is validated on the hardware in section 6.

5.2. Effect of body height

Next, we consider whether the superior performance of sideways walking is unique to the height we have chosen. To do this, we consider two slices of the full 3D workspace at the bottom of figure 3(a) for h = 18 and 19 cm, respectively, and find their maximum SL. In order to do so, for sideways walking, we consider a ZY plane through the center of the workspace in figure 3(a). For forward walking, we consider a XZ plane through the widest part of the



workspace in figure 3(a). In the same way, the stride planes for different heights, figures 6(a) and (b), the maximum SL at each height can be observed, and is plotted in figure 6(c). Note that when height is greater than 10 cm, front and rear legs have the same maximum SL as the middle leg's, as shown with the isosceles triangle in figure A1. However, when the height is less than 10 cm, the full stride limits are different for middle and front/rear legs.

For both forward walking and sideways walking, a step that holds the body at a constant height of less 10 cm will be limited in size based on the joint angle limits (see how the workspace plot tapers at the top of figures 6(a) and (b)). Limiting factors include the rotational joints and AGD limits, and the front and rear legs rotating 45° with respect to normal to the body. In particular, for sideways walking, the workspace of is non-contiguous if the height is below 10 cm, suggesting that the robot could take small steps with large *y* position (>20 cm, highly sprawled) or small steps with *y* < 15 cm, but would not be able to move between these regions within a single stance. This suggests a lower limit on walking height based on joint angle limits.

For walking with body height above 10 cm, the available SLs are different for forward walking and sideways walking. For forward walking, figure 6(b), there is a maximum SL near 10 cm, and a gradual decrease at higher heights. For sideways walking, the maximum SL is at closer to 14 cm height, with a steeper decrease at higher body heights.

We can only validate kinematic predictions for the upper range of body heights, due to limitations of highly sprawled postures for our physical robot in sand, and we focus our simulation in this range. Since the height is the measured from the center of the hip joint, when the height is too low the chassis drags along the ground. This is exacerbated when the dactyls penetrate the sand. The gray bar in figure 6(c) shows the appropriate height ranges for our robot experimentally. Fortunately, that range includes a critical intersection at which forward walking SLs exceed SLs of sideways walking. Thus, we tested this limited height range at three points (17.5 cm when the sideways SLs are longer, 19 cm when the forward walking SLs are longer, and 18 cm when they are approximately equal). This represents the upper height range possible since at 20 cm, the workspace tapers to zero.

For all three of the heights examined, sideways walking is faster, and energetically superior. The differences become smaller when the height is larger, and sideways walking worsens. Specifically, the speed of the sideways walking robot is 73% faster at the lowest height and 40% faster at the highest height. The COT of the forward walking robot is 127% higher at the lowest height and only 56% higher at the highest height.

Overall, the best walking is expected to be sideways walking at the lowest possible body height, 17.5 cm. Perhaps in future hardware designs, legs could be mounted below chassis and sand penetration could be limited with dactyl design to enable even more sprawled posture comparisons at heights close to 14 cm. However, heights below 10 cm would not be desirable with current joint and angle limits.

6. Results

We compared three gaits: the full stride gaits for sideways and forward walking (the best possible gaits), and a half stride sideways gait, figures 3(b) and (c). This half stride gait should be comparable to the forward gait at full stride since our prediction was that



the sideways gait was roughly twice as good. In addition, such a gait with shorter-than-maximum steps could be a valuable baseline for realtime SL adaptation in the presence of obstacles [18]. The period for

half SL sideways gait is 1.2 seconds, as opposed to the

period for full sideways gait of 1.5 seconds (table 2) and is determined in the same method.

Sideways and forward walking are compared in four progressively more realistic evaluations from kinematic prediction, to simulation, to walking on



hard floors, to walking in dry sand, which represents one of the more challenging terrains for crab-like robots.

First, the kinematic prediction of velocity is calculated using equation (1), with the SL and period determined as above. As is clear from figure 7(a), the kinematic predictions of the speed for forward and sideways walking are similar. Thus, dynamics are needed to understand the differences.

Secondly, based on the dynamic simulation results in Webots, figure 7(a), when the interaction with a smooth low-friction ground is included, forward walking is much slower than sideways walking and slower than the kinematic prediction, as shown in the previous section. A contributing factor is the degree of slip between the dactyl and the ground. Specifically, while the middle legs tend to have small slip, the front and rear legs for forward walking have a high amount of backward slip, which we diagram in figure 8. In sideways walking, middle legs slip slightly more than front and back legs, since it is opposed by two legs, however the degree of slip is less. Additionally, forward walking involves more lateral motion of the body, which does not occur in sideways walking.

The average velocity for the full stride sideways walking is 62% larger than the half stride sideways gait, which validates that the full SL gait yields the









optimal gait. Note that low-friction environment was chosen because it simplifies modeling (especially compared to granular media), and can be directly compared with walking on the lab floor (i.e. the solid bars in figure 7(a) are similar to the shaded bars).

Thirdly, we validate these simulation results with physical hardware, our robot Sebastian. For each gait, we did ten trials of ten strides each on the linoleum floor and kept all parameters the same as the simulation.

The hardware trials validate the velocity predictions from Webots. Specifically, the Webots predictions are 95% accurate. The slight difference may caused by the error from the fabrication, servos' motion, power sensor and parts connection of Sebastian. This supports our conclusion that the fastest sideways walking gait is *1.05 body lengths per second, 75% faster than the fastest forward walking gait, figure 7(a).

Although the forward walking COT is in the range reported by other hexapod robots, e.g. [101], walking sideways lowers COT by 40%, as shown in figure 7. One possibility was that the lower COT is due to the fact that sideways walking only uses two joints per leg (ankle and knee) whereas forward walking uses three (ankle, knee and hip). To investigate whether this is the case, we separated the energy contribution of each joint for each gait, figure 9(a). This calculation is from ten full strides of the simulation joint torques, which is expected to be similar to hardware due to the overall similarity of COT in figure 7. As expected, the energy used by swinging legs is less than the energy used by stance legs (since leg mass is small relative to body mass). However, one potentially surprising result is that even without the energy used by the hip joint, sideways walking is still more efficient, since the knee

and ankle require more energy for forward walking. This is true despite the fact that the knee and ankle move more than (full stride) or comparable to (half stride) forward walking, figure 9(b).

Thus, we conclude that in addition to the number of joints utilized, the higher COT is due to energy lost from slip, figure 8 and other dynamic effects, including rotation of the body, figure C1.

Finally, we tested the robot on dry sand, figure 10, since granular media is a natural substrate for crablike locomotion. The sand is Pavestone natural play sand. The robot walked in ten directions in the sand tank to minimize any error caused by differences in the sand surface. For each gait, we did ten trials in sand and kept all parameters the same. Every trial includes ten full strides.

For all gaits, sand slows down the robot, which is consistent with other papers [30, 31]. The COT is also increased, as expected, because of the resistance of the sand, increased slip, and more variable and unstable steps. Forward gait velocity performance reduction percentages are lower than sideways walking, because the sand reduces the slippage on the front and rear legs when compared with the linoleum tests in appendix B.

Nonetheless, the full stride sideways gait is both faster and more energy efficient than the full stride forward gait in sand. A half stride sideways gait is comparable to the full stride forward gait in efficiency and speed.

7. Conclusions

Taken together, our results suggest sideways walking at the lowest height, utilizing the full range of motion is best for energy efficiency and speed. By both metrics, sideways walking appears better than forward walking. Sideways is more efficient and faster at all heights in the range of our robot. Sideways is better on flat smooth terrain and on dry granular media. Sideways gives better speed per SL. Sideways gives longer SLs at low heights. The single exception seems to be that forward walking enables longer SLs when the robot is at its maximum height but not enough to translate into faster or more efficient walking.

In addition, we demonstrate a gait design method that is effective in variable terrains. On tile floor, sideways walking is comparable to kinematic and simulation predictions. On sand, as expected, all the robot gaits are slower and less efficient. However, the relative speeds and efficiency on sand follow the same patterns. This suggests that the gait design method is sufficiently generalizable to varying terrain. Since beaches are of particular interest for crab robots, testing on rocky and wet substrates will be interesting for future work. However, our prior work [30, 31] suggests that compact wet sand may be easier to traverse than dry sand since wet sand is strengthened by capillary forces, and the increase in shear strength can reduce leg slip. Thus, our experiments here are meant to convey the best and worst case for walking on beaches, showing sideways walking is superior in both.

This work reflects the differences in a common leg design configuration for forward walking robots [76, 82–86, 89, 90]. The fact that it is common for forward walking makes it all the more surprising that sideways walking is more efficient and reflects an opportunity to use these already designed robots differently.

8. Discussion

8.1. Comparison with biology

Biological crabs are diverse and able to traverse a wide range of terrains [102]. As is visible from table 3, some species are larger, and some are smaller than our hexapod robot. Inhabiting a range of ecological niches, they also display a wide range of walking speeds, both above and below the speed of our robot when normalized by leg length [103–105, 105–108]. The crabs closest in size to our robot are king crabs, like Paralomis formosa [103–105] and Kamchatka crabs [105, 106]. Since the reported studies are ecological rather than biomechanical, some of the walking recorded could include sideways walking. However, like all king crabs, their joint anatomy enables forward walking rather than the sideways walking characteristic of true crabs of order Brachyura [105]. The king crabs have a speed to leg length ratio of around 3, which is similar to our robot's forward walking

speed to leg length ratio of 4. Meanwhile, examples of *Brachyura* crabs are much faster, in the case of the ghost crabs, reflecting fast muscle actions and dynamic gaits in which the step length is extended by jumping through the air [109]. As walking robots improve to serve in tedious and hazardous tasks, bio-inspiration from crabs can provide important insights.

Our robot's preference for sideways walking is consistent with evolutionary biology [66]. In multiple instances forward walking animals have developed sideways-walking crab-like anatomy in a process called carcinization [65]. Sideways walking is thought to help the animal walk faster, but may reduce the pleon and claw size [65].

8.2. Fundamental trade-offs for sideways and forward walking

Our robotic experiments suggest that a preference for sideways walking may be due to mechanical differences in sideways and forward walking that are shared between robots and animals. There are several key differences in walking directions fundamental to both robots and animals.

First, forward walking uses three joints per leg, while sideways walking only relies on two, since the hip angle can be constant during sideways walking. Using the hip joint for forward walking contributes to the energy cost (15%, figure 9) but does not result in an increase overall speed. This is not to say that hip joints are not valuable. The tests in this paper use a fixed gait, but animals and robots in challenging terrain can use a hip joint in footfall planning and maneuvering in both forward and sideways walking. Therefore, there are advantages to having DOF available that are not used in nominal walking, and future study could investigate this further.

Second, sideways walking enables qualitatively different use of the dactyls. Sideways walking keeps dactyls in a plane, while forward motion rotates dactyl. This is pictured in figures 8 and 10. While in both cases the AGD limits are the same, in sideways walking the dactyls can rotate to follow the curve of the dactyls, almost rolling like a wheel over the terrain, which can be seen in appendix B and figure 10. For the three legs in the front, this motion may help slide over terrain. For the three legs in the rear, this might help compact the granular media before push off. In contrast, in forward walking, the dactyls rotate sideways during stance, digging the tips out as the AGD increases, figure 10 and appendix B. Loosening the terrain around the dactyl may make it harder to anchor to the ground in surf zones. There may also be trade-offs for probing the substrate or burrowing in granular media.

Thirdly, forward walking induces more body rotation and dactyl slip. While the slip at the middle legs,

Species	Mass (kg)	Leg length (cm)	$\frac{\text{velocity}}{\text{leg length}} \left(\frac{\text{mm/s}}{\text{cm}}\right)$	Preferred walking direction	References
Pachygrapsus crassipes	0.02	5	17 ^a	Sideways	[110-112]
Ghost crab	0.05	9	178	Sideways	[113–115]
Paralomis formosa	0.23	23	3	Forward	[103-105]
Kamchatka crab	8	150	3 ^a	Forward	[105, 106]
Red king crab	10.9	152	0.1	Forward	[107, 116]
Coconut crab	37.3	123	50	Forward	[108, 117]
Our robot	3.65	29	7	Sideways	This paper
Our robot	3.65	29	4	Forward	This paper

Table 3. Normalized velocity for Sebastian robot and several crab species.

^aThe average velocity is used. Maximum velocities are used for others. Note that these speeds are from a variety of sources from laboratory [110, 113] tests to migrations [103, 107], and are only provided to demonstrate the impressive range of animal scales.

shown in figure 8, are small and comparable, the slip of the other legs can be greater, figure 8. In particular in forward walking, the impacts of the alternating tripods are asymmetric at the onset of stance due to the fact that two feet fall on one side and one on the other side. Two legs on the right (+Y) land at the same time as the middle leg on the left (-Y), causing a COM displacement to the left (-Y), which will be corrected in the next alternating tripod [118–120]. While these offsets are small relative to the body width of the robot, as shown in figure C1 in appendix C, they can introduce wasted yaw rotation that is not present in sideways walking [121]. Both yaw rotation and slippage from front and rear legs, figure 8, result in smaller velocity of forward walking, which is visible in figure C1, and evident in lower energy efficiency. One reason that the decrease in energy efficiency from tile to sand is smaller for forward walking might be that the sand damps this oscillation. Compliance in the leg may be an important factor to consider in future.

8.3. Limitations and future work

A limitation of this study is that because a complete optimization of leg morphology and gait control was not performed, we cannot rule out the possibility that there could exist a faster forward gait, especially for the sand. Our approach has the advantage that the robot motions are constrained to be slow enough to be precise, which means that they could be adjusted for precise foot placement. If this constraint was lifted, and more variable path parameterization was used, a more complete and detailed optimization would be possible. However, such an optimization seems unlikely to double the speed of forward walking. If such an optimization was performed either *a priori* or during walking, the approach presented here provides a heuristic for an appropriate baseline.

Furthermore, our results could be sensitive to leg design. Our robot segment lengths were chosen based on a goal to grasp rocky terrain by taking advantage of valleys between spheres [122], it may be that optimizing the legs for forward walking will yield improved forward walking gaits. This may be an area in which the study of biological crabs will be relevant, especially since our calculated optimal corresponds to the leg ratio which is also found in sideways walking crabs [122]. Actuators inspired by artificial muscles may be able to provide different behaviors.

Even more, the end effector design can be a factor. Simpler end effectors might not be able to take advantage of the sideways rolling motion of the dactyls. Compliant end effectors can recover and store impact energy. End effectors with variable friction or attachment properties could be exploited to a greater degree with more adaptive control. Sensing could enable closed-loop slip reduction gaits.

Interesting future work would be to compare studies of different number of legs [123–133] or different leg configurations. For example, some robots are configured for agile omnidirectional walking [53–55], and may have spectrum of gaits that includes forward and sideways walking, unlike here in which sideways and forward walking represent qualitatively different behaviors.

While we hope this study encourages use of sideways walking gaits in future robots, we recognize that there are disadvantages for sideways walking. Having legs on the "sides" as in forward walking (rather than the front and back for sideways walking) means that sensors are not occluded by the legs. For example, mounting cameras and range finders on the front of the robot can enable careful footfall planning for forward waking. However, in surf zone, sand and water, vision may be less helpful than tactile exploration, which can explain why crabs but not insects use sideways walking. Another advantage of forward walking is that legs can be specialized for a forward motion [134], unlike for crabs which typically walk equally well left and right. An insect might use rear legs for power and forward legs for manipulation and a lobster can balance front claws and rear pleon. However, in robot design, having multiple redundant parallel legs with the same design can be robust and cost-effective.







(C) Simulation vs linoleum vs sand for all three gaits: in "Sim_vs_Linoleum_vs_Sand.mov"

(D) Simulation vs linoleum for all Gaits in "Sim_vs_linoleum_vs_sand.mov"

Figure B1. The overview of the main videos provided in the link.

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Data availability statement

The data that support the findings of this study are openly available at the following URL/DOI: https://drive.google.com/drive/folders/177CMm GKD1x23WKgBmd5N7fL3iEMmehJE.

Appendix A. The full stride lengths for front, rear and middle legs are the same

See Figure A1.

Appendix B. The videos of Webots dynamic simulation and Sebastian walking on linoleum floor and sand for all three gaits—full stride sideways and forward walking, and half stride sideways walking

See (Figure B1).

Appendix C. The tracks of the center of mass of Sebastian within two cycles

See Figure C1.

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